

## WORKSHOP 8

### Objectives:

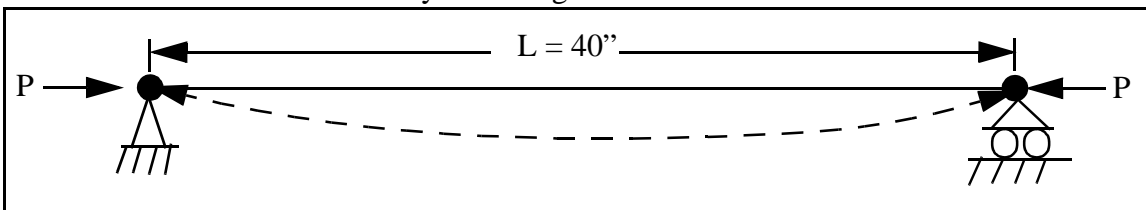
- Design a structure with strength and buckling limits
- Impose three buckling conditions
  - (a) The MSC.Nastran buckling analysis
  - (b) Euler Buckling Equation Limit

$$\sigma \geq \sigma_{cr}^{Eul} = \frac{-\pi^2 E}{(L'/\rho)^2}$$

- (c) Johnson Short Columns Design Formula

$$\sigma \geq \sigma_{cr}^{John} = -\sigma_{co} \left[ 1.0 - \frac{\sigma_{co} (L'/\rho)^2}{4\pi^2 E} \right]$$

- Use the beam library in a design task.



For the pinned-pinned condition and a rod cross section type:

$$L' = L$$

$$\rho = \frac{r}{2} \quad (\rho = \text{radius of gyration})$$

Assume  $\sigma_{co} = +80,000$ . ( $\sigma_{co}$  is an empirically determined column yield stress)



## Model Description:

- Subject to:
  - Static load of -200,000 at grid point 6
  - pins at points 1 and 6
  - Buckling Analysis
- Objective Functions: Minimize the Weight
- Design variable: Radius of rod
- Constraints:

Static Case:

- $-80,000 \leq \sigma \leq 100,000$

- $\sigma \geq \sigma_{cr}^{EUL}$

- when  $-\sigma > \frac{\sigma_{co}}{2}$  \*

$$\sigma \geq \sigma_{cr}^{John}$$

Buckling Subcase:

$$\lambda \geq 1.0$$

\*The Johnson Condition is the critical design condition only if the magnitude at the compressive stress is greater than  $\sigma_{co}/2$ . This can be implemented in MSC.Nastran by multiplying the response by a factor that is the maximum of 0.0 and  $(-\sigma - \sigma_{co}/2)$ . When the maximum is 0.0, the Johnson condition is ignored.

---

# Generating an input file for MSC.Nastran Users:

1. Generate an input file using the data from pages 8-1 through 8-3. Use the following input file as a starting point.

```
ID MSC, wkshp8a
TIME 130      $
SOL 200      $ OPTIMIZATION
CEND
TITLE      = buckling test case
SUBTITLE   = johnson/euler buckling case
ECHO      = SORT
spc       = 100
DESOBJ    = 20
SUBCASE 1
  DESSUB   = 1
  LABEL    = LOAD CONDITION 1
  LOAD     = 300
  ANALYSIS = STATICS
  DISP    = ALL
  STRESS  = ALL
SUBCASE 2
  DESSUB   = 2
  ANALYSIS = BUCK
  METHOD    = 1
  DISP     = ALL
  LABEL    = BUCKLING FACTORS
$
BEGIN BULK
param,post,-1
$-----
$ ANALYSIS MODEL
$-----
$
$ GRID DATA
$      2      3      4      5      6      7      8      9      10
GRDSET      345
grid      1      0.0      0.0      0.0
grid      2      8.0      0.0      0.0
grid      3      16.0     0.0      0.0
grid      4      24.0     0.0      0.0
grid      5      32.0     0.0      0.0
grid      6      40.0     0.0      0.0
grid      10     0.0      0.0      100.0      123456
$
$ ELEMENT AND MATERIAL DATA
cbar      1      10      1      2      10
cbar      2      10      2      3      10
cbar      3      10      3      4      10
cbar      4      10      4      5      10
cbar      5      10      5      6      10
MAT1      1      3.0e7      0.33      0.1
$ PROPERTY DATA
PbarL    10      1      mscbml0rod
          1.0
$ BOUNDARY CONDITION DATA
spc1     100      1      1
spc1     100      2      1      6
$ EXTERNAL LOADS DATA
FORCE    300      6      -2.0e5      1.0
```

## WORKSHOP 8

---

```
$ BUCKLING ANALYSIS DATA
EIGRL      1      .05      4
$
$-----
$ DESIGN MODEL
$-----
$
$ Beginning of Design Modeling Exercise for the Bulk Data Section
$
.
.
.
$
ENDDATA
```

## 2. The completed MSC.Nastran input file is shown below:

```

ID MSC, soln8a
TIME 130      $
SOL 200      $ OPTIMIZATION
CEND
TITLE      = buckling test case
SUBTITLE   = johnson/euler buckling case
ECHO      = SORT
spc       = 100
DESOBJ    = 20
SUBCASE 1
  DESSUB  = 1
  LABEL   = LOAD CONDITION 1
  LOAD    = 300
  ANALYSIS = STATICS
  DISP    = ALL
  STRESS  = ALL
SUBCASE 2
  DESSUB  = 2
  ANALYSIS = BUCK
  METHOD   = 1
  DISP    = ALL
  LABEL   = BUCKLING FACTORS
$
BEGIN BULK
param,post,-1
$-----
$ ANALYSIS MODEL
$-----
$
$ GRID DATA
$      2      3      4      5      6      7      8      9      10
GRDSET
grid 1          0.0  0.0      0.0
grid 2          8.0  0.0  0.0
grid 3          16.0 0.0  0.0
grid 4          24.0 0.0  0.0
grid 5          32.0 0.0  0.0
grid 6          40.0 0.0  0.0
grid 10         0.0  0.0  100.0      123456
$
$ ELEMENT AND MATERIAL DATA
cbar 1  10    1    2    10
cbar 2  10    2    3    10
cbar 3  10    3    4    10
cbar 4  10    4    5    10
cbar 5  10    5    6    10
MAT1   1  3.0e7      0.33  0.1
$ PROPERTY DATA
PbarL  10    1      mscbml0rod
      1.0
$ BOUNDARY CONDITION DATA
spc1 100  1    1
spc1 100  2    1    6
$ EXTERNAL LOADS DATA
FORCE 300    6      -2.0e5  1.0
$ BUCKLING ANALYSIS DATA
EIGRL  1      .05      4
$
$-----

```

## WORKSHOP 8

```

$ DESIGN MODEL
$-----
$
DESVAR 1      rg1.0      0.01      10.0
DOPTPRM p2  15      DESMAX 20      DELP 0.5      GMAX 0.01
        CONV DV 0.01      CONVPR 0.02      p1 1
DRESP1 20      W      WEIGHT
DRESP1 23      S1      STRESS Pbar      7      10
DRESP1 24      S1      STRESS Pbar      8      10
DRESP1 25      S1      sTRESS Pbar      6      10
dresp2 31      EUL      31
        DESVAR 1
        DTABLE L      E
        DRESP1 25
$ EULER CONSTRAINT CONDITION
deqatn 31      rgyra(r,l,e,sigma) = r / 2.0;
        euler = - sigma * ( L / rGYRA ) **2 / (PI(1)**2 * E)
dresp2 32      JOHNSON 32
        DESVAR 1
        DTABLE L      E      SIGMAC
        DRESP1 25
$
$ JOHNSON CONSTRAINT CONDITION THAT IS ONLY ACTIVE WHEN FAC IS NONZERO
$
deqatn 32      LORHO2(r,l,e,SIGMAC,sigma) = (2.0 * L / R ) ** 2;
        fac = max((-sigma - sigmac/2.0), 0.0);
        JOHNSON = - FAC * sigma / ((-sigma - sigmac/2.0) *
        SIGMAC * ( 1.0 - SIGMAC * LORHO2/
        (4.0 * PI(1)**2 * E) ) )
DCONSTR 1 23      100000.
dconstr 1 24      -80000.
dconstr 1 31      1.0
dconstr 1 32      1.0
dtable e 30.0e6      1      40.0      sigmac      8.0e4
DVPREL1 10 pbar1      1012
        1 1.0
$
$ DESIGN FOR BUCKLING EIGENVALUE
DRESP1 1      BUCK1 LAMA      1
dconstr 2 1      1.0
param dsnokd 1.0
$
ENDDATA

```

- 
3. Submit the input file to MSC.Nastran for analysis.

To submit the MSC.Nastran **.dat** file, find an available UNIX shell window and at the command prompt enter **nastran wkshp8 scr=yes**. Monitor the run using the UNIX **ps** command.

4. When the run is completed, edit the **wkshp8.f06** file and search for the word **FATAL**. If no matches exist, search for the word **WARNING**. Determine whether existing WARNING messages indicate modeling errors.

- 4a. While still editing **wkshp8.f06**, search for the word:

H I S T O R Y

# Comparison of Results:

- Compare the results obtained in the .f06 file with the following:

```

GO
SUBCASE 2
*****
SUMMARY OF DESIGN CYCLE HISTORY
*****
(HARD CONVERGENCE ACHIEVED)
(SOFT CONVERGENCE ACHIEVED)
NUMBER OF FINITE ELEMENT ANALYSES COMPLETED 3
NUMBER OF OPTIMIZATIONS W.R.T. APPROXIMATE MODELS 2
OBJECTIVE AND MAXIMUM CONSTRAINT HISTORY
-----
CYCLE  NUMBER  INITIAL  OBJECTIVE FROM  FRACTIONAL ERROR  MAXIMUM VALUE
APPROXIMATE  EXACT  OF
OPTIMIZATION  ANALYSIS  APPROXIMATION  CONSTRAINT
-----
INITIAL  1.256637E+01
1  1.539844E+01  1.539775E+01  4.471775E-05  3.485799E-03
2  1.540468E+01  1.540468E+01  1.238162E-07  2.788901E-03
-----
BUCKLING TEST CASE
JOHNSON/EULER BUCKLING CASE
NOVEMBER 10, 1999 MSC.NASTRAN 10/11/99 PAGE 71
SUBCASE 2
DESIGN VARIABLE HISTORY
-----
INTERNAL | EXTERNAL | LABEL | INITIAL : 1 : 2 : 3 : 4 : 5 :
DV. ID. | DV. ID. | 1 : 2 : 3 : 4 : 5 :
1 | 1 | RG | 1.0000E+00 : 1.1069E+00 : 1.1072E+00 :
*** USER INFORMATION MESSAGE 6464 (DOM12E)
RUN TERMINATED DUE TO HARD CONVERGENCE TO AN OPTIMUM AT CYCLE NUMBER = 2.

```

6. Use the output produced by DOPTPRM parameter p2 = 15 to determine the critical design case in the .f06 file, search for **FINAL**. Then search again for **DESIGN CONSTRAINTS**. This will lead to a table like:

```

----- DESIGN CONSTRAINTS ON RESPONSES -----
(MAXIMUM RESPONSE CONSTRAINTS MARKED WITH **)
-----
INTERNAL RESPONSE ID DCONSTR ID INTERNAL RESPONSE TYPE L/U FLAG INTERNAL REGION ID SUBCASE ID VALUE
-----
1 2 1 1 STRESS LOWER 1 1 -3.5085E-01
2 3 1 1 STRESS LOWER 1 1 -3.5085E-01
3 4 1 1 STRESS LOWER 1 1 -3.5085E-01
4 5 1 1 STRESS LOWER 1 1 -3.5085E-01
5 6 1 1 STRESS LOWER 1 1 -3.5085E-01
6 1 1 1 EQUA UPPER 31 1 -8.4299E-02
7 2 1 1 EQUA UPPER 31 1 -8.4299E-02
8 3 1 1 EQUA UPPER 31 1 -8.4299E-02
9 4 1 1 EQUA UPPER 31 1 -8.4299E-02
10 5 1 1 EQUA UPPER 31 1 -8.4299E-02
11 6 1 1 EQUA UPPER 32 1 2.7889E-03**
12 7 1 1 EQUA UPPER 32 1 2.7889E-03**
13 8 1 1 EQUA UPPER 32 1 2.7889E-03**
14 9 1 1 EQUA UPPER 32 1 2.7889E-03**
15 10 1 1 EQUA UPPER 32 1 2.7889E-03**
16 12 2 1 LAMA LOWER 0 2 -8.6330E-02
----- CONSTRAINTS ON DESIGNED PROPERTIES -----

```

# WORKSHOP 8

This indicates that five constraints are tied at the maximum value and that they are associated with an EQUA response type and have internal ID's 6 thru 10.

Search for RETAINED DRESP2. This leads to a table like:

```

----- RETAINED DRESP2 RESPONSES -----
-----
INTERNAL  DRESP2  RESPONSE  EQUATION  LOWER  UPPER
  ID      ID      LABEL      ID        BOUND  BOUND
-----
    1     31     EUL       31        N/A    1.0000E+00
    2     31     EUL       31        N/A    1.0000E+00
    3     31     EUL       31        N/A    1.0000E+00
    4     31     EUL       31        N/A    1.0000E+00
    5     31     EUL       31        N/A    1.0000E+00
    6     32     JOHNSON  32        N/A    1.0028E+00
    7     32     JOHNSON  32        N/A    1.0028E+00
    8     32     JOHNSON  32        N/A    1.0028E+00
    9     32     JOHNSON  32        N/A    1.0028E+00
   10     32     JOHNSON  32        N/A    1.0028E+00
-----
  
```

---

It is seen that the maximum constraints are associated with the Johnson condition.

7. Repeat the workshop problem with  $L = 60$ . How do the answers change and what is the critical design condition?